

**TCS II**  
**Formal Languages and Computability 2018/19**  
**1st Midterm (B)**

8. April 2019

Solve the assignments on your own.

Time limit is 80 minutes.

Good luck!

ASSIGNMENT	POINTS	OUT OF	ASSIGNMENT	POINTS	OUT OF
1			2		
3			4		

FIRST AND LAST NAME: \_\_\_\_\_

STUDENT ID: \_\_\_\_\_

SIGNATURE: \_\_\_\_\_

**1. Assignment:** (30 points)

Let's define languages:

$$L_1 = \{0^n w \mid w \text{ is an arbitrary string containing 0's and 1's, of length } n\}, \Sigma = \{0, 1\}$$

$$L_2 = \{w \mid a^* b (aa + c)^*\}, \Sigma = \{a, b, c\}$$

**QUESTIONS:**

For every language:

1. Find out if the language is regular or not, justify your claim!

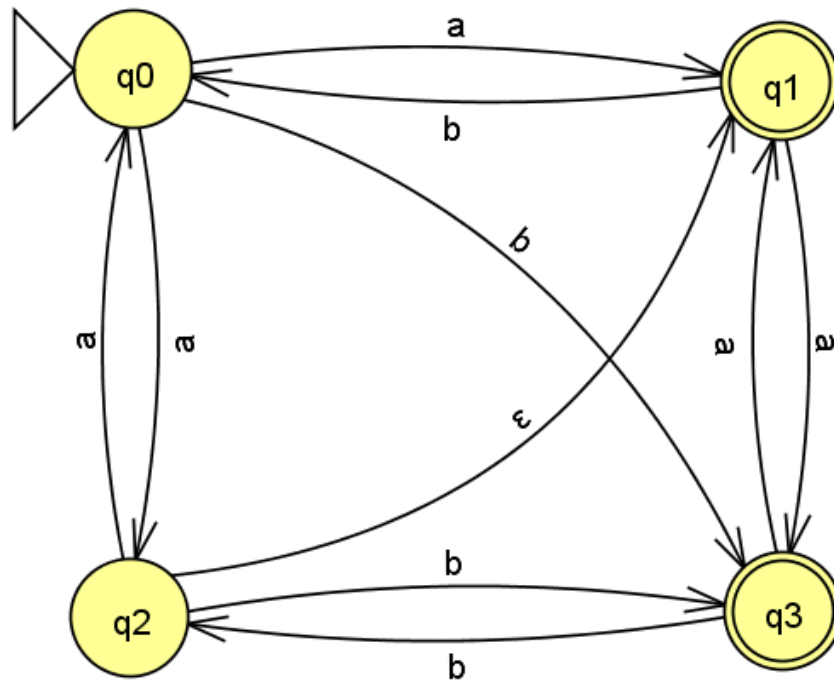
**INSTRUCTIONS:**

If a language is regular, construct a deterministic finite automaton (DFA) – write down the complete 5-tuple. If the language is not regular, you must prove that such an automaton cannot be constructed (pumping lemma for regular languages).

2. For every language, define a context free grammar (CFG) for it.

**2. Assignment:** (20 points)

You are given the following  $\epsilon$ -NFA:

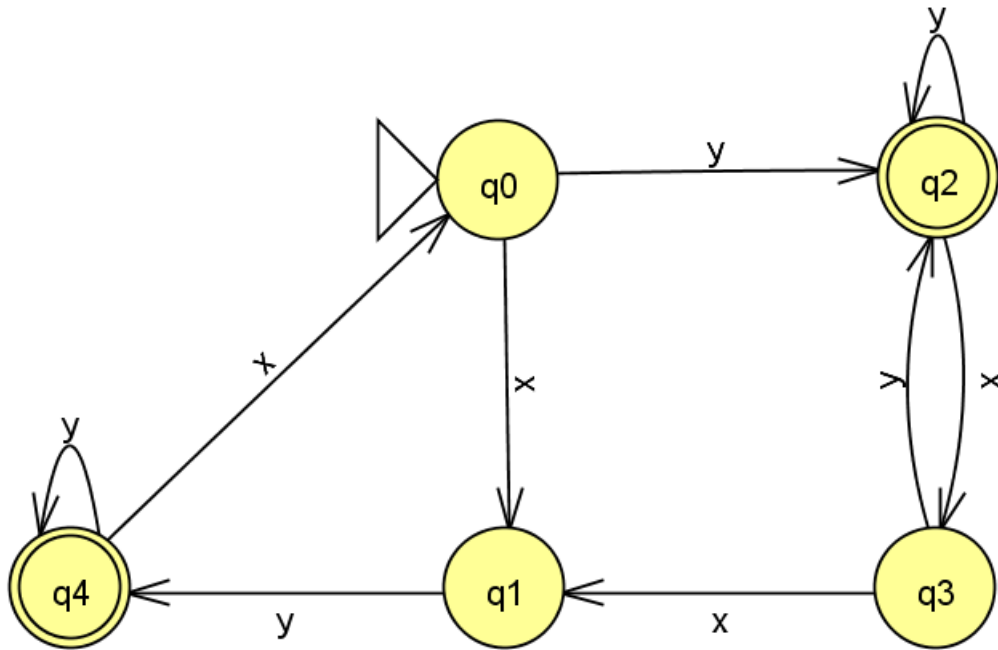


**QUESTIONS:**

Transform the  $\epsilon$ -NFA to a DFA using the procedure(s) shown in class.

**3. Assignment:** (25 points)

You are given the following automaton:



**QUESTIONS:**

Minimize the automaton using the table filling method.

**4. Assignment:** (25 points)

You are given the following context free grammar (CFG),  $\Sigma = \{a, b, c\}$ :

$$S \rightarrow ABC \mid AB \mid BCD$$

$$A \rightarrow aaAa \mid BbA \mid \varepsilon$$

$$B \rightarrow A \mid bB$$

$$C \rightarrow Cc \mid c$$

$$D \rightarrow aD \mid bDc$$

**QUESTIONS:**

Turn this grammar into Chomsky Normal Form (CNF) – write down the complete procedure.